# C rystal structure determination and ab initio molecular structure prediction for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, the first phosphorus selenide cyanide 

Bruce W. Tattershall,* E mma L. Sandham and W illiam C legg<br>Department of Chemistry, University of Newcastle, N ewcastle upon Tyne NE 1 7RU, UK


#### Abstract

Bicyclic exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2} \mathbf{1}$ was made by reaction of $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3} \mathrm{I}_{2}$ with AgCN , and its crystal structure determined from X-ray data collected at 160 K . M olecular structures were predicted for ex 0, exo $-\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$ and $\mathrm{P}_{2} \mathrm{Se}_{5} 2$ by restricted H artree-Fock ab initio molecular-orbital calculations using STO3G, 3-21G* and L anL 2D Z (d) ECP basis sets, and for $\mathrm{P}_{2} \mathrm{Se}_{5}$ additionally using A hlrichs' split-valence and triplezeta valence basis sets. Comparisons with the crystal structure of exo, exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ and with a previously published crystal structure of $\mathrm{P}_{2} \mathrm{Se}_{5}$ showed that the $3-21 \mathrm{G} *$ basis sets gave sufficiently good predictions for most bond angles that the effects on them of intermolecular interactions in the crystals could be discussed.


$M$ olecules exo, exo- $\alpha-P_{4} E_{3} R^{1} R^{2}$, where $E=S$ or Se and $R^{1}$ and $R^{2}=H$, halide or carbon-, nitrogen-, phosphorus- or sulfurcentred substituents, have been studied in solution by ${ }^{31} \mathrm{P}$ NM R spectroscopy. ${ }^{1-6}$ This can provide detailed information about molecular structure, particularly about bond angles, but only when relationships between coupling constants or chemical shifts and geometric parameters have been established empirically. U ntil now, the only compounds in the series which have yielded crystals suitable for structure determination have been the iodides $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3} I_{2}$ and $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}{ }_{2}{ }_{2}{ }^{7,8}$ To obtain structural data for correlation with N M R results we have therefore begun to predict molecular geometries by ab initio molecular orbital (MO) methods, using the program GAUSSIAN 94. ${ }^{9}$ Semiempirical or molecular modelling methods are not possible because of lack of parametrisation for molecules with polycyclic phosphorus chalcogenide skeletons.

M ost reported ab initio work involving phosphorus has been aimed at testing the efficiency of increasingly sophisticated basis sets. Thus, A hlrichs and co-workers ${ }^{10,11}$ have optimised an improved split-valence (SV) basis $\{(10 \mathrm{~s}, 7 \mathrm{p}) /[4 \mathrm{~s}, 3 \mathrm{p}]$ for P or S ; $(14 s, 10 p, 5 d) /[5 s, 4 p, 2 d]$ for Se$\}^{10}$ and a basis of valence triplezeta (TZV) quality $\{(14 s, 9 p) /[5 s, 4 p]$ for $P$ or $S$; $(17 s, 13 p, 6 d) /$ [ $6 s, 5 p, 2 d$ ] for Se \}. ${ }^{11}$ (In this notation the number of G aussiantype primitive functions is in parentheses, and the number of functions into which they are contracted is in square brackets. To calculate the number of orbitals, the number of $p$ functions should be multiplied by three and that of d functions by five.) These bases were tested using only very simple molecules, though the SVP set for phosphorus (SV augmented by one set of d polarisation functions) was recently used extensively for calculations on polyphosphane rings. ${ }^{12}$ In previous work on selenium and other third-row atoms Binning and Curtiss calculated split-valence bases ( $14 s, 11 p, 5 d) /[6 s, 4 p, 1 d]$ and tested them in predicting several measured properties of simple molecules. ${ }^{13}$ They concluded that simpler 3-21G* bases yielded molecular geometries which, in terms of differences from experimental geometries, were of similar quality $\{3-21 \mathrm{G}$ is a ( $12 \mathrm{~s}, 9 \mathrm{p}, 3 \mathrm{~d}$ )/ [ $5 s, 4 p, 1 d]$ contraction for Se , with corresponding $s$ and $p$ exponents constrained to be equal\}. In calculations of NMR chemical shifts using the gauge-including atomic orbital method, less contracted basis sets have been used: ( $12 \mathrm{~s}, 9 \mathrm{p}$ )/ [ $6 s, 5 p]$ for phosphorus ${ }^{14}$ and ( $14 \mathrm{~s}, 11 \mathrm{p}, 5 \mathrm{~d}$ )/[9s,6p,2d] for selenium. ${ }^{15}$ In both cases, polarisation functions were added, and, for selenium, diffuse functions were also needed to account for the lone pairs of electrons.

For chemical shift calculations at least singlepoint all-
electron calculations are required, since much of the nuclear shielding is by core electrons, but for calculations of geometry effective corepotential (ECP) methods can in principle be used. H ere, model potential s are substituted for core electrons, so that the number of basis functions is reduced. This offers little advantage for the second-row elements since time saved at the self-consistent field (SCF) stage is compensated by extra time spent at the gradient calculation stage, of each geometry optimisation cycle In test calculations of the geometry of $\mathrm{P}_{4} \mathrm{~S}_{3}$, constrained to $\mathrm{C}_{3 v}$ symmetry, we found the following comparative times for one cycle of geometry optimisation: STO-3G, 88 s; 3-21G*, 317 s; A hlrichs' SV P, 430 s ; LanL 2D Z(d) (a double zeta ECP basis with one added d polarisation function), ${ }^{16} 691 \mathrm{~s}$. In contrast, for molecules containing many selenium atoms, the LanL 2DZ(d) basis allows remarkably faster geometry optimisation even than 3-21G* (see below).
In contrast to most of the above work, we wished to make calculations on many molecules, each containing at least seven second-row atoms, as well as more or less complex exocyclic substituents centred on first-row atoms. In order to do this as an adjunct to preparative and NM R spectroscopic research, within modest use of supercomputer time and of man-hours spent in servicing the computations, we decided to resort to simpler basis sets than those developed recently. This should be possible as our aim was not to calculate accurate absolute energies or values of geometric or NMR parameters, but rather to calculate comparisons between similar molecules, or even between similar sites within a molecule. In such cases, systematic errors caused by use of small basis sets may be expected to cancel out to some extent. We found at an early stage that the minimal basis set STO-3G is of little use, since it gives qualitatively unrealistic geometries for nitrogen-centred substituents bonded to phosphorus. ${ }^{17}$ (For the molecules reported here, where substantial $\pi$ bonding to phosphorus is not expected, ST 0-3G calculations were a useful intermediate stage, and are reported.) Since most of our work involved molecules with phosphorus sulfide skeletons, we opted to use 3-21G* basis sets in restricted Hartree-Fock (RHF) calculations as a probable best compromise, and have calculated geometries which have been useful in rationalising trends in N M R parameters in several cases. ${ }^{17,18}$ However, a comparison of a predicted molecular structure with a measured structure is desirable, to verify that the results are reasonably realistic.

We now report the synthesis of the first phosphorus selenide cyanide, exo, exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2} \mathbf{1}(\mathrm{E}=\mathrm{Se})$, which yielded well formed crystals, enabling an X-ray diffraction analysis.

Table 1 Phosphorus-31 NMR data ${ }^{\text {a }}$ for exo,exo- $\alpha-P_{4} E_{3}(C N)_{2}(E=S e$ or S)

|  | $E=S e$ | $E=S^{\text {b }}$ |
| :---: | :---: | :---: |
| $\delta\left(\mathrm{P}_{\mathrm{A}}\right)$ | 106.16 | 128.69 |
| $\delta\left(\mathrm{P}_{\mathrm{B}}\right)$ | 29.17 | 34.18 |
| ${ }^{2} \mathrm{~J}\left(\mathrm{P}_{\mathrm{A}} \mathrm{P}_{\mathrm{C}}\right)$ | 95.73(7) | 86.3 |
| $\left.{ }^{1}\right]\left(P_{A} P_{B}\right)$ | -252.11(5) | -254.7 |
| ${ }^{2} \mathrm{~J}\left(\mathrm{P}_{\mathrm{A}} \mathrm{P}_{\mathrm{D}}\right)$ | 34.63(3) | 32.1 |
| ${ }^{3} \mathrm{~J}\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{D}}\right)$ | -19.26(4) | -14.4 |

a Solvent: $\mathrm{CS}_{2}$. Chemical shifts are in ppm relative to $\mathrm{H}_{3} \mathrm{PO}_{4}$-water and coupling constants are in Hz with standard deviations $(\sigma)$ in parentheses. A tom labelling is shown in Scheme 1. ${ }^{\mathrm{b}} \mathrm{R}$ ef. 1.

A lthough the molecule presented its own difficulties in ab initio structure prediction, this has now been accomplished. U se of a 3-21G* basis set gives a geometry which is very similar to that found in the crystal. We also report, for comparison, predictions of molecular geometry for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$.

While the bicyclic molecule $\mathrm{P}_{2} \mathrm{Se}_{5} \mathbf{2}$ is an isolated case offering no sites for exocyclic substitution and hence empirical correlations, its crystal structure has been reported. ${ }^{19}$ Its molecular geometry is sufficiently similar to that of the skeleton of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ for useful comparisons to be made. We have therefore further tested use of the 3-21G* basis set for selenium compounds by predicting the structure of $\mathrm{P}_{2} \mathrm{Se}_{5}$. We verified that much better agreement with the crystal structure geometry was not produced by more expensive calculations using Ahlrichs' SVP or TZVP+ basis sets. The LanL 2D Z(d) ECP method gave similar results to the $3-21 G *$ basis for all three molecules.

## Results and discussion

## Synthesis of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$

The analogous compound exo, exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$ was first made by Fluck et al. ${ }^{20}$ by stirring a solution of $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3} \mathrm{I}_{2}$ in $\mathrm{CS}_{2}$ with solid A gCN over 5 d at $50^{\circ} \mathrm{C}$. This silver salt method of making compounds $\alpha-P_{4} E_{3} X_{2}$ offers the possibility of yielding a pure solution of the product, since the Agl formed is extremely insoluble. The sulfide cyanide was always accompanied, however, by substantial impurities, ${ }^{1}$ a minor one of which was later identified as the invertomer endo, ex $0-\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$, ${ }^{6}$ and crystals suitable for structure determination could not be obtained.

In contrast to this, $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3} \mathrm{I}_{2}$ reacted completely with an excess of AgCN at room temperature $\left(20^{\circ} \mathrm{C}\right)$ in 5 d , to give a solution containing only exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{I}) \mathrm{CN}$, exo,exo- $\alpha$ $\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ 1, and endo, exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, in molar ratio 48:29:23. F urther stirring of the mixture at $52^{\circ} \mathrm{C}$ for 1 d then caused the complete further reaction of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(I) \mathrm{CN}$ and disappearance of all but a trace of endo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, to leave exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ as the only phosphoruscontaining solute in significant concentration. The solution was saturated without further concentration, and a sample taken at $42^{\circ} \mathrm{C}$ gave well formed yellow crystals on slow cooling to $20^{\circ} \mathrm{C}$. A full N M R study including all three products will be reported separately as part of a larger work: ${ }^{21}$ only the chemical shifts and coupling constants from the main ${ }^{31}$ P NMR spectrum of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ are included here for identification purposes. Table 1 shows that these compare well with corresponding parameters for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$. The lower value of $\delta\left(\mathrm{P}_{\mathrm{A}}\right)$ in the selenium compound may be attributed to the effect of the lower electronegativity of two neighbouring selenium atoms.

## C rystal structure

The asymmetric unit consists of a single complete molecule, which thus has no crystallographic symmetry. The essential

(b)


Fig. 1 Crystal packing of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ 1, showing interactions (a) between stacks and (b) along a stack. D istances in $\AA$
symmetry of the molecule, but not of its crystalline environment, is $\mathrm{C}_{2}$. The complete molecular geometry is given in Table 2 and views of it in Fig. 1.

## Ab initio molecular structure prediction

A molecular geometry for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ with $\mathrm{C}_{2}$ symmetry was derived from the observed non-symmetric geometry in the crystal, by averaging corresponding pairs of bond lengths or angles required for a $Z$ matrix. Starting from this, ab initio geometry optimisation was performed with $\mathrm{C}_{2}$ symmetry imposed, first at the RHF/STO-3G, then at the RHF/3-21G* level. A major difficulty resulted from the near-linearity of the $\mathrm{P}-\mathrm{C}-\mathrm{N}$ chains. The average bond angle at carbon in the crystal was $173.6^{\circ}$ and was predicted in the free molecule to be 177.12 (ST O-3G) or $177.36^{\circ}(3-21 G *)$. This resulted in a rather flat energy minimum with respect to rotation about the $\mathrm{P}-\mathrm{C}$ bond. The geometry of the $\mathrm{P}_{4} \mathrm{Se}_{3}$ skeleton varied little once it had approached the optimum, but it depended sufficiently on the orientation of the CN group to make us reluctant to fix arbitrarily the rotational position. The convergence tests built in to GAUSSIAN 94 were eventually satisfied only when the newly available redundant internal coordinates method, rather than Z-matrix variable optimisation, was used, and then only after 29 optimisation cycles at the STO-3G level and 18 at the 3-21G* level. Similar difficulties were encountered in corresponding calculations for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$. For both molecules, the calculations were confirmed by reoptimisation using the Los A lamos LanL 2DZ(d) ECP basis sets. Relative times for one (final) cycle of geometry optimisation using the STO-3G, 3-21G* and ECP bases were 317, 1942 and 2315 s for exo,exo- $\alpha$ $\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, or 94 (Z-matrix method), 899 and 1989 s for exo,exo- $\alpha-P_{4} S_{3}(C N)_{2}$.
$U$ sing the redundant internal coordinate method for $\mathrm{P}_{2} \mathrm{Se}_{5}$, only 31 geometric parameters are optimised (of which five are independent under $C_{2 v}$ symmetry), compared with 51 for exo,-exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$. This, together with the absence of difficulties caused by exocyclic substituents, made $\mathrm{P}_{2} \mathrm{Se}_{5}$ a suitable molecule for which to study the use of more sophisticated basis sets. Geometry optimisation was carried out using A hlrichs' SVP or TZVP + bases, or the LanL2D Z(d) ECP basis (see Table 2 footnotes), in addition to using the STO-3G or 3-21G* bases. Relative times for one cycle of geometry optimisation, with symmetry constrained to $C_{2 v}$, were $248,1190,2700,5192$ and 575 s , for the STO-3G, 3-21G*, SVP, TZVP + and ECP basis


1


2

Scheme 1 Labelling of atoms for exo,exo- $\alpha-P_{4} E_{3}(C N)_{2} \mathbf{1}(E=S$ or Se $)$ and $\mathrm{P}_{2} \mathrm{Se}_{5} 2$
sets. Prediction of the geometry of $\mathrm{P}_{2} \mathrm{Se}_{5}$ raised the question of whether the free molecule necessarily has $\mathrm{C}_{2 v}$ symmetry. It seemed possible that the six-membered ring might adopt a twist-boat rather than a simple boat configuration, depending on what distance $P_{A} \cdots P_{c}$ (Scheme 1) $\dagger$ was best stabilised by the $\mathrm{Se}_{\mathrm{a}}$ bridge. This would result in the selenium atoms of the six-membered ring forming two pairs related by $\mathrm{C}_{2}$ symmetry. The non-equivalent atoms within each pair would differ only in long-range interactions within the molecule; e.g. the distances $\mathrm{Se}_{\mathrm{a}} \cdots \mathrm{Se}_{\mathrm{b}}$ and $\mathrm{Se}_{\mathrm{a}} \cdots \mathrm{Se}_{\mathrm{B}}$ would be different. There would therefore be a low-energy path for deformation through the boat form with $\mathrm{C}_{2 v}$ symmetry to the enantiomer twisted in the opposite sense, and it would not be surprising that all selenium atoms in the six-membered ring appear chemically equivalent on the NMR time-scale, ${ }^{22}$ even at 240 K . ${ }^{23}$ To investigate this, we constrained the ab initio optimisations of geometry for $\mathrm{P}_{2} \mathrm{Se}_{5}$ only to $\mathrm{C}_{2}$ rather than to $\mathrm{C}_{2 v}$ symmetry in calculations using the ST 0-3G, 3-21G * or ECP bases, but Table 2 shows that the twist angle $P_{A}-\mathrm{Se}_{\mathrm{B}}-\mathrm{Se}_{\mathrm{b}}-\mathrm{P}_{\mathrm{c}}$ is predicted to be zero, probably to within the accuracy of these methods. The $\mathrm{C}_{2 \mathrm{v}}$ symmetry is thus confirmed. The twist angles found in the crystal structure were much larger and of opposite sign, ${ }^{19}$ corresponding to a deformation giving a substantial difference in 'book angles' $\mathrm{Se}_{\mathrm{B}}{ }^{-}$ $\mathrm{P}_{\mathrm{A}}-\mathrm{Se}_{\mathrm{d}}$ and $\mathrm{Se}_{\mathrm{b}}-\mathrm{P}_{\mathrm{c}}-\mathrm{Se}_{\mathrm{D}}$ (108.44 and $104.88^{\circ}$ ). This seems very unlikely in the free molecule and was not tested in the present calculations. In the crystal structure it is readily attributable to intermolecular Se…Se and P... Se interactions, discussed below.

## C omparison of measured and predicted structures

Bond lengths and angles and a selection of torsion angles predicted by ab initio calculation for exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$, exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$ and $\mathrm{P}_{2} \mathrm{Se}_{5}$ are compared in Table 2 with values from the crystal structures of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ and $\mathrm{P}_{2} \mathrm{Se}_{5}$.

For $\mathrm{P}_{2} \mathrm{Se}_{5}$ the root mean square (r.m.s.) deviation between predicted and measured bond angles was $1.68,1.11,0.97,0.92$ and $0.98^{\circ}$, using the STO-3G, $3-21 \mathrm{G}^{*}$, SVP, TZVP + and ECP basis sets respectively. There was some balancing of deviations in bond angles. If angles in the crystal structure which would be equal under $\mathrm{C}_{2 v}$ symmetry were averaged, then the r.m.s. deviations from the ab initio predictions, of these averaged values, had lower values for the five basis sets: $1.44,0.70,0.47,0.35$ and $0.49^{\circ}$. Corresponding r.m.s. deviations for bond lengths from individual crystal values were $0.020,0.019,0.014,0.015$ and $0.018 \AA$ compared with $\sigma$ values of about $0.002 \AA$ for the crystal structure data. A s anticipated by the designers of the SVP basis set, ${ }^{10}$ there is little useful extra accuracy of geometrical parameters to be gained, in RHF calculations, by spending

[^0](a)



(c)




Fig. 2 Crystal packing of $\mathrm{P}_{2} \mathrm{Se}_{5} 2$ (from atomic coordinates in ref. 19), showing interactions (a) between chains (b) along a chain and (c) between layers. D istances in $\AA$
nearly twice as much computer time in going from the SVP to the TZVP + basis. If the TZVP+ geometry is assumed to be 'correct' for the free molecule, then, while bond lengths and non-bonded lengths are generally too short from 3-21G* calculations, bond angles, which are the most useful parameters on which to base qualitative discussion of observed N M R results, are predicted accurately enough at the $3-21 \mathrm{G}$ * level. At less than half the computer-time requirements of the SVP basis, our choice of the $3-21 \mathrm{G}$ * level for the rest of the calculations is thus justified. N one of the arguments below about the effect of crystal interactions, based on the 3-21G* geometry, needed to be changed to agree with the result of the TZVP + calculation. The STO-3G model was not sufficiently accurate to be used as a basis for these arguments. In the particular case of a compound with several selenium atoms and relatively few internal geometric coordinates, the ECP method is clearly to be preferred over any of the others.
M ost of the larger deviations from predictions at the 3-21G* level for $\mathrm{P}_{2} \mathrm{Se}_{5}$ can be explained in terms of intermolecular interactions in the crystal. Thus, intermolecular $\mathrm{Se} \cdots \mathrm{Se}$ interactions, at 3.53 and $3.52 \AA$, act on $\mathrm{Se}_{\mathrm{B}}$ and $\mathrm{Se}_{\mathrm{d}}$ respectively approximately collinearly with their intramolecular bonds to $\mathrm{P}_{\mathrm{A}}$, so as to have little effect on bond angles, but on $\mathrm{Se}_{\mathrm{D}}$ and $\mathrm{Se}_{\mathrm{b}}$ approximately normally to their bonds to $\mathrm{P}_{\mathrm{c}}[\mathrm{Fig} .2(\mathrm{a})]$. This causes a decrease in book angle $\mathrm{Se}_{\mathrm{D}}-\mathrm{P}_{\mathrm{c}}-\mathrm{Se}_{\mathrm{b}}$ to less than its value in the free molecule. A nother set of intermolecular interactions exists between $\mathrm{Se}_{\mathrm{a}}$ in one molecule and $\mathrm{P}_{\mathrm{A}}$ and $\mathrm{Se}_{\mathrm{d}}$ (both at 3.62 $\AA$ ) in the next, to form chains nearly collinear with the intra-

Table2 (continued)


| $\begin{aligned} & \text { STO-3G } \\ & \mathrm{C}_{2} \end{aligned}$ | $\begin{aligned} & 3-21 G^{*} \\ & \mathrm{C}_{2} \end{aligned}$ | $\begin{aligned} & \text { ECPb } \\ & C_{2} \end{aligned}$ |
| :---: | :---: | :---: |
| 51.05 | 51.80 | 51.36 |
| 50.00 | -47.68 | -48.34 |
| 51.05 | 51.80 | 51.36 |
| -50.00 | -47.68 | -48.34 |
| 67.62 | 65.89 | 67.31 |
| -73.83 | -78.04 | -76.73 |
| 67.62 | 65.89 | 67.31 |
| -73.83 | -78.04 | -76.73 |
| 3.01 | 7.44 | 5.76 |
| 132.68 | 133.13 | 130.22 |
| -122.77 | -123.08 | -125.89 |
| 3.01 | 7.44 | 5.76 |
| 132.68 | 133.13 | 130.22 |
| -122.77 | -123.08 | -125.89 |



[^1]molecular $\mathrm{Se}_{\mathrm{a}}-\mathrm{P}_{\mathrm{A}}$ bonds [Fig. 2(b)]. This causes an opening of the intramolecular book angle $\mathrm{Se}_{\mathrm{B}}-\mathrm{P}_{\mathrm{A}}-\mathrm{Se}_{\mathrm{d}}$ to greater than the free-molecule value, to make room for the distant selenium to interact with $P_{A}$, while the five-membered ring angle $\mathrm{Se}_{\mathrm{a}}-$ $\mathrm{P}_{\mathrm{A}}-\mathrm{Se}_{\mathrm{d}}$ is compressed. The other partner in this interaction, $\mathrm{Se}_{\mathrm{a}}$, is displaced intramolecularly in the direction of $P_{A}$, increasing the bond angle at $\mathrm{Se}_{\mathrm{a}}$. Longer intermolecular interactions (at 3.64 and $3.66 \AA$ ) exist between layers [ Fig . 2(c)]. If the interaction $\mathrm{Se}_{\mathrm{D}} \cdots \mathrm{Se}_{\mathrm{b}}$ is repulsive, but $\mathrm{P}_{\mathrm{A}} \cdots \mathrm{Se}_{\mathrm{B}}$ is attractive, an increase in bond angle at $\mathrm{Se}_{\mathrm{b}}$ and a decrease in that at $\mathrm{Se}_{\mathrm{B}}$ is explained

The larger molecule exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ is affected by a much more complex network of intermolecular interactions in the crystal. The r.m.s. deviations between predicted and crystal geometry were $2.4,1.8$ and $1.8^{\circ}$ for bond angles, and 0.009 , 0.010 and $0.019 \AA$ for bond lengths, at the ST O-3G, 3-21G * and ECP levels. A s for $\mathrm{P}_{2} \mathrm{Se}_{5}$, bond lengths predicted using the ECP basis were too long, and for exo, exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ those predicted using the $3-21 \mathrm{G} *$ basis were nearer to those measured in the crystal. The ECP and 3-21G* bases gave predictions of similar accuracy, as judged by comparison with crystal data, of some bond angles, but for others the geometry in the crystal is clearly strongly perturbed, compared with either prediction for the free molecule. The following discussion will be based on the $3-21 \mathrm{G}$ * predictions. In contrast to the $\mathrm{P}_{2} \mathrm{Se}_{5}$ case, molecules stack with their approximate $\mathrm{C}_{2}$ axes aligned with the $b$ crystallographic axis [Fig. 1(b)]: the shortest interaction along the stack, between $\mathrm{Se}_{\mathrm{a}}$ and $\mathrm{Se}_{\mathrm{b}}$ in the next molecule, is long ( $3.92 \AA$ ) and the stack seems to be held together mainly by stronger interactions with molecules in both directions along neighbouring stacks [Fig. 1(a)]. Several of these involve nitrogen or $\mathrm{P}_{\mathrm{B}}$ (or $P_{D}$ ), which are predicted at the RHF/3-21G* level to carry significant charges ( -0.41 and +0.51 respectively). While the environments of $P_{B}, P_{A}$ and $\mathrm{Se}_{d}$ are different from those of $P_{D}$, $\mathrm{P}_{\mathrm{c}}$ and $\mathrm{Se}_{\mathrm{b}}[\mathrm{Fig} .1(\mathrm{a})]$, the effect of intermolecular interactions, in contrast to the $\mathrm{P}_{2} \mathrm{Se}_{5}$ case, is to close both book angles $\mathrm{P}_{\mathrm{D}}-\mathrm{P}_{\mathrm{c}}-\mathrm{Se}_{\mathrm{b}}$ and $\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{A}}-\mathrm{Se}_{\mathrm{d}}$, rather than to close one and open the other. The contact between $\mathrm{Se}_{\mathrm{d}}$ and a distant $\mathrm{P}_{\mathrm{c}}$ (at $3.58 \AA$ ) is the shortest of the clearly book-closing interactions. Distant nitrogen atoms interact with $\mathrm{Se}_{b}, \mathrm{P}_{\mathrm{B}}, \mathrm{Se}_{d}$ and $\mathrm{P}_{\mathrm{D}}$ at 3.38, 3.31, 3.31 and $3.18 \AA$, but are almost in the approximate planes of the $P_{A}-P_{B}-\mathrm{Se}_{\mathrm{b}}-\mathrm{P}_{\mathrm{c}}$ or $\mathrm{P}_{\mathrm{c}}-\mathrm{P}_{\mathrm{D}}-\mathrm{Se}_{\mathrm{d}}-\mathrm{P}_{\mathrm{A}}$ half rings. Instead of closing the book angles, these interactions may be responsible for compressing the half rings so as to open the six-membered ring angles at $\mathrm{Se}_{b}, \mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{D}}$, with widening of the angle at $\mathrm{Se}_{\mathrm{a}}$. The opening of the ring angles is augmented for $P_{D}$ and is rendered negligible for $\mathrm{Se}_{\mathrm{d}}$ by a strong intermolecular interaction ( $3.29 \AA$ ) between atoms $\mathrm{P}_{\mathrm{D}}$ on neighbouring enantiomeric molecules. This acts approximately along the line of the $P_{D}-\mathrm{Se}_{\mathrm{d}}$ bond and has no counterpart on the $\mathrm{P}_{\mathrm{B}}$ side of the molecule. Bond length $\mathrm{P}_{\mathrm{D}}-\mathrm{Se}_{\mathrm{d}}$ is rendered shorter than $\mathrm{P}_{\mathrm{B}}-\mathrm{Se}_{\mathrm{b}}$ The shortness of the $P_{D} \cdots P_{D}$ contact may reflect a decrease in the van der Waals radius of $P_{D}$, associated with its positive charge. While interactions with $N_{d}$ are nearly along the line of the $\mathrm{P}-\mathrm{C}-\mathrm{N}$ sequence, those with $\mathrm{N}_{\mathrm{b}}$ have the effect of closing angle $\mathrm{Se}_{\mathrm{b}}-\mathrm{P}_{\mathrm{B}}-\mathrm{C}_{\mathrm{b}}$.

## Comparison between predicted structures for exo,exo- $\alpha$ $P_{4} S_{3}(C N)_{2}$ and exo,exo- $\alpha-P_{4} S_{3}(C N)_{2}$

Calculations using the 3-21G* and ECP bases gave almost identical skeletal bond angles to each other for exo,exo- $\alpha$ $\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$. Changes in endocyclic bond angles in going from predicted values for exo, exo $-\alpha-\mathrm{P}_{4} \mathrm{~S}_{3}(\mathrm{CN})_{2}$ to thosefor exo, exo- $\alpha$ $\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2}$ are very similar to changes in the corresponding angles in going from the measured crystal structure of $\alpha-\left.\mathrm{P}_{4} \mathrm{~S}_{3}\right|_{2}$ to that of $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}{ }_{2}{ }^{2}{ }^{7,8}$ The distance $\mathrm{S}_{\mathrm{a}} \cdots \mathrm{S}_{\mathrm{b}}$ or $\mathrm{S}_{\mathrm{a}} \cdots \mathrm{S}_{\mathrm{d}}$ in the sulfur compound is, at $3.303 \AA$ ( $3-21 \mathrm{G} *$ results, Table 2), much shorter than the sum of the van der Waals radii ( $3.60 \AA$ ), Replacing sulfur by selenium forces an increase in separation of
the chalcogen nuclei to $3.547 \AA$, compared with a radius sum of $3.80 \AA$. This can be accomplished only by decreases in bond angles at all three chalcogen atoms. The decreases are larger than on going from crystalline $\mathrm{S}_{8}$ to crystalline $\mathrm{Se}_{8}$, where comparable repulsions do not exist. Within the five-membered rings, the decreases are compensated by increases in bond angles at all three phosphorus atoms, including $P_{B}$ (or $P_{D}$ ) even though non-bonded distances $\mathrm{P}_{\mathrm{B}} \cdots \mathrm{E}_{\mathrm{a}}$ (3.310 changing to $3.434 \AA$ ) and $\mathrm{P}_{\mathrm{B}} \cdots \mathrm{E}_{\mathrm{d}}$ ( 3.243 changing to $3.309 \AA$ ) are also within the van der Waals radius sums ( 3.65 changing to $3.75 \AA$ ). The sum of bond angles at the bridgehead atoms $\mathrm{P}_{\mathrm{A}}$ or $\mathrm{P}_{\mathrm{C}}$ increases by $2.26^{\circ}$. Opening of the book angles is probably resisted by lone-pair repulsion at the bridgehead atoms (valence shell electron pair repulsion effect), and possibly by an attractive interaction $P_{B} \cdots E_{d}$. As noted above, crystal forces appear capable of further reducing the book angles in the selenium compound, so as to return $\mathrm{P}_{\mathrm{B}} \cdots \mathrm{P}_{\mathrm{D}}$ to a value close to that for the sulfur compound.

Despite changes in endocyclic bond lengths and angles at $\mathrm{P}_{\mathbf{B}}$ or $P_{D}$, the bond lengths and angles to carbon are practically unaffected by chalcogen substitution, as is the geometry of the cyanide group. This is in contrast to the crystal structures of the iodides, where replacement of sulfur by selenium results in an increase in bond angles to iodine. It probably shows that, in contrast to iodine, cyanide has little intramolecular nonbonded interaction with the molecular skeleton.

## Experimental

## Preparation of exo,exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathbf{C N})_{2} \mathbf{1}(\mathbf{E}=\mathbf{S e})$

Silver cyanide was freshly prepared by addition of $\mathrm{AgNO}_{3}-$ water to KCN-water, with care that the final solution was not alkaline It was washed with ethanol and dried by pumping at high vacuum for 3 h at $20^{\circ} \mathrm{C}$. All subsequent operations were carried out under nitrogen, using Schlenk methods. The compound $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3} \mathrm{I}_{2}$ was made by reaction of stoichiometric quantities of red P , grey Se and $\mathrm{I}_{2}$ in a sealed ampoule at $240-300^{\circ} \mathrm{C}$ over 3 d , followed by Soxhlet extraction using $\mathrm{CS}_{2}$.

Silver cyanide ( $1.071 \mathrm{~g}, 8.00 \mathrm{mmol}$ ) was added to crystalline $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3} \mathrm{I}_{2}(0.615 \mathrm{~g}, 1.00 \mathrm{mmol})$ and the mixture stirred vigorously with $\mathrm{CS}_{2}\left(20 \mathrm{~cm}^{3}\right)$ for 5 d at $20^{\circ} \mathrm{C}$, then at $52^{\circ} \mathrm{C}$ for 24 h , with protection from light. During this second stage the solution changed from mid-yellow to almost colourless. The temperature was reduced to $42^{\circ} \mathrm{C}$ for sampling of the supernatant liquid by pipette to a clean Schlenk tube. This was allowed to cool slowly in a large oil-bath to $20^{\circ} \mathrm{C}$, when crystals of exo, exo- $\alpha-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2} \mathbf{1}(\mathrm{E}=\mathrm{Se})$ were obtained and removed by pipette. The NMR spectra of solutions were measured in 10 mm diameter tubes with a precision capillary containing $\left(\mathrm{CD}_{3}\right)_{2} \mathrm{CO}$ for locking, using a Bruker WM 300WB spectrometer operating at 121.5 M Hz for ${ }^{31} \mathrm{p}$. Spectra were fitted using the program NUMARIT. ${ }^{24}$

## X-R ay crystallography

Crystal data for exo,exo- $\boldsymbol{\alpha}-\mathrm{P}_{4} \mathrm{Se}_{3}(\mathrm{CN})_{2} \mathbf{1}(\mathbf{E}=\mathbf{S e}) . \mathrm{C}_{2} \mathrm{~N}_{2} \mathrm{P}_{4} \mathrm{Se}_{3}$, $M=412.80$, monoclinic, space group $P 22_{1} / c, a=13.898(2)$, $b=6.3903(11), c=11.882(2) \AA, \beta=109.397(4)^{\circ}, U=995.4(3)$ $\AA^{3}, Z=4, D_{c}=2.755 \mathrm{~g} \mathrm{~cm}^{-3}, \mu=11.67 \mathrm{~mm}^{-1}(\mathrm{M} 0-\mathrm{K} \alpha$, $\lambda=0.71073 \AA), F(000)=752, T=160 \mathrm{~K}$.

A yellow crystal of size $0.50 \times 0.38 \times 0.06 \mathrm{~mm}$ was examined on a Siemens SMART CCD area-detector diffractometer. Intensities were integrated from several series of frames covering $0.3^{\circ}$ each in $\omega$, the total data set corresponding to morethan a hemisphere of reciprocal space. Remeasurement of the initial frames at the end of data collection indicated no significant change in intensity. Semiempirical absorption corrections were applied, based on repeated and symmetry-equivalent reflections in the data set (transmission 0.121-0.623). 3603 M easured
reflections yielded 1616 unique data with $\mathrm{R}_{\text {int }}=0.0853$ and $\theta_{\text {max }}=25.31^{\circ}$.

All atoms were located by direct methods and were refined with anisotropic displacement parameters by full-matrix leastsquares methods based on $\mathrm{F}^{2}$, with the weighting scheme $\mathrm{w}^{-1}=\sigma^{2}\left(\mathrm{~F}_{0}{ }^{2}\right)+(0.0567 \mathrm{P})^{2}+(1.6241 \mathrm{P})$, where $\mathrm{P}=\left(2 \mathrm{~F}_{\mathrm{c}}{ }^{2}+\mathrm{F}_{0}{ }^{2}\right) / 3$. An isotropic extinction parameter $x$ refined to $0.0025(5)$, whereby $F_{c}$ is multiplied by $\left(1+0.001 x F_{c}{ }^{2} \lambda^{3} / \sin 2 \theta\right)^{-1 / 4}$. At convergence, $R^{\prime}=\left[\Sigma w\left(F_{o}{ }^{2}-F_{c}{ }^{2}\right)^{2} / \Sigma w\left(F_{o}{ }^{2}\right)^{2}\right]^{1 / 2}=0.1097$ for all data, conventional $R=0.0385$ on $F$ values of 1459 reflections having $F_{0}{ }^{2}>2 \sigma\left(F_{o}{ }^{2}\right)$, goodness of fit $=1.121$ on $F^{2}$ for all data and 101 refined parameters. Extremes of the final difference map were +0.64 and -1.04 e $\AA^{-3}$. Programs: Siemens SM ART and SAINT control and integration software, SHELXTL. . ${ }^{25}$

A tomic coordinates, thermal parameters, and bond lengths and angles have been deposited at the Cambridge Crystallographic D ata C entre (CCDC). See Instructions for Authors, J. Chem. Soc., Dalton Trans., 1996, Issue 1. A ny request to the CCDC for this material should quote the full literature citation and the reference number 186/258.

## Acknowledgements

We thank the EPSRC for provision of X -ray equipment (to W. C.) and for a grant of vector supercomputer resources (to B. W. T.) for ab initio calculations. Dr M. N. S. Hill is thanked for assistance in obtaining NMR spectra, and Dr M. R.J. Elsegood for assistance in analysis of the crystal packing.

## References

1 B. W. Tattershall, J. Chem. Soc., D alton Trans., 1987, 1515.
2 B. W. Tattershall, J. Chem. Soc., D alton Trans., 1991, 483.
3 R. Blachnik, K. Hackmann and H.-P. Baldus, Z. N aturforsch., Teil B, 1991, 46, 1165.
4 R. Blachnik and K. Hackmann, Phosphorus Sulfur Silicon Relat. Elem., 1992, 65, 99.
5 B. W. Tattershall and N. L. K endall, J. Chem. Soc., Dalton Trans., 1993, 3163.

6 B. W. Tattershall and N. L. K endall, Polyhedron, 1994, 13, 1507.
7 D. A. Wright and B. R. Penfold, A cta Crystallogr., 1959, 12, 455; B. W. Tattershall, N. L. K endall, A . M cCamley and W. Clegg, A cta C rystallogr., Sect. C, 1993, 49, 571.
8 R. Blachnik, G. K urz and U. Wickel, Z. N aturforsch., Teil B, 1984, 39, 778.
9 M. J. Frisch, G. W. Trucks, H. B. Schlegel, P. M. W. Gill, B. G. Johnson, M. A. Robb, J. R. Cheeseman, T. K eith, G. A. Petersson, J. A. M ontgomery, K. R aghavachari, M . A. AI-L aham, V. G. Zakrzewski, J. V. Ortiz, J. B. Foresman, J. Cioslowski, B. B. Stefanov, A. N anayakkara, M. Challacombe, C. Y. Peng, P. Y. Ayala, W. Chen, M. W. Wong, J. L. A ndres, E. S. Replogle, R. Gomperts, R. L. M artin, D. J. Fox, J. S. Binkley, D. J. D efrees, J. Baker, J. P. Stewart, M. Head-Gordon, C. Gonzalez and J. A. Pople, GAUSSIAN 94, Revision B.1, Gaussian Inc., Pittsburgh, PA, 1995.
10 A. Schäfer, H. H orn and R. A hlrichs, J. C hem. P hys., 1992, 97, 2571.
11 A. Schäfer, C. Huber and R. A hlrichs, J. Chem. Phys., 1994, 100, 5829.

12 S. Böcker and M. H äser, Z. A norg. Allg. Chem., 1995, 621, 258.
13 R. C. Binning, jun. and L. A . Curtiss, J. Comput. Chem., 1990, 11, 1206.

14 D. B. Chesnut and B. E. Rusiloski, C hem. Phys., 1991, 157, 105.
15 M. Bühl, W. Thiel, U. F leischer and W. K utzelnigg, J. Phys. Chem., 1995, 99, 4000.
16 W. R. Wadt and P. J. H ay, J. Chem. Phys., 1985, 82, 284.
17 B. W. Tattershall and E. L. Sandham, Z. A norg. Allg. Chem., 1996, 622, 1635.
18 R. Blachnik, K. H ackmann and B. W. Tattershall, Polyhedron, 1996, 15, 1415.
19 R. Blachnik, P. Lönnecke, K. Boldt and B. Engelen, A cta Crystallogr., Sect. C, 1994, 50, 659.
20 E. Fluck, N. Yutronic S. and W. H aubold, Z. A norg. Allg. Chem., 1976, 420, 247.
21 B. W. Tattershall and E. L. Sandham, unpublished work.
22 H.-P. Baldus, R. Blachnik, P. Loennecke and B. W. Tattershall, J. Chem. Soc., D alton Trans., 1991, 2643.

23 B. W. Tattershall, J. Lutz and R. Blachnik, unpublished work.
24 A. R. Quirt, J. S. M artin and K. M. Worvill, N UM ARIT, Version 771, SERC N M R Program Library, D aresbury, 1977.
25 G. M. Sheldrick, SHELXTL U sers' M anual, Version 5, Siemens A nalytical X-R ay Instruments, M adison, WI, 1994.

Received 17th J une 1996; Paper 6/04230


[^0]:    $\dagger$ For purposes of comparison, for $\alpha-P_{4} E_{3}(C N)_{2} \mathbf{1}$, similar atom labelling has been used throughout this paper as in previous NMR-based papers (e.g. ref. 5); $\mathrm{P}_{2} \mathrm{Se}_{5} 2$ has been labelled to correspond to this.

[^1]:     $0.0348, \mathrm{Se} 0.0220$ ). ${ }^{\mathrm{f}}$ Torsion angle A-B-C-D is the angle between projections of vectors BA and CD on a plane perpendicular to BC

